

NMR Strukturbestimmung

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Inhalt

1. Konformationsdaten aus NMR Messungen
2. Strukturbeschreibung mit Atomkoordinaten oder Torsionswinkel
3. Strukturbestimmung: grundsätzliche Möglichkeit, praktische Schwierigkeiten
4. Strukturberechnungsalgorithmen: interaktiver Modellbau, Distanzgeometrie, Optimierung einer Zielfunktion, Simulated Annealing, Moleküldynamiksimulation, Torsionswinkeldynamik
5. Darstellung von NMR Strukturen: Strukturbündel, RMSDs
6. Automatisierung der NOE-Zuordnung und Strukturberechnung
7. Strukturanalyse: Übereinstimmung mit experimentellen Daten, Verletzungen von Konformationseinschränkungen, RMSD, Ramachandranplot, Validierung

Konformationsdaten aus NMR Messungen

Konformationsdaten aus NMR Messungen

1. NOEs
2. 3J skalare Kopplungen
3. H-Brücken
4. Chemische Verschiebungen
5. Residuelle dipolare Kopplungen (RDC)
- ...

NOE (Nuclear Overhauser Effect)

NMR Daten: Integral V von NOESY Kreuzsignalen
 Konformationsdaten: obere Schranken für ^1H - ^1H Distanzen, d
 Fuer isoliertes Spinpaar im starren Molekül:

$$V = C/d^6 \quad \text{mit } C = \text{konstant}$$

Eigenschaften:

- nur kurze Distanzen < 5 Å messbar
- dichtes Netzwerk bzgl. der Sequenz kurz- und langreichweiterer Distanzschranken
- viele ^1H Atome im Molekül → "Spindiffusion"
- interne Bewegungen → nicht-lineare Mittelung
- Bestimmung der Konstanten C ?
- Überlapp → mehrdeutige Zuordnung, verfälschte Integrale

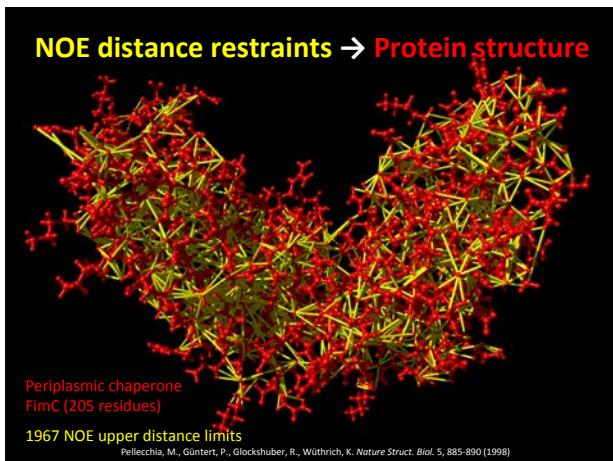
NOE Calibration

$$V = C / d^6$$

Volume of NOESY cross peak
 "Calibration constant"
 Distance (upper distance bound)

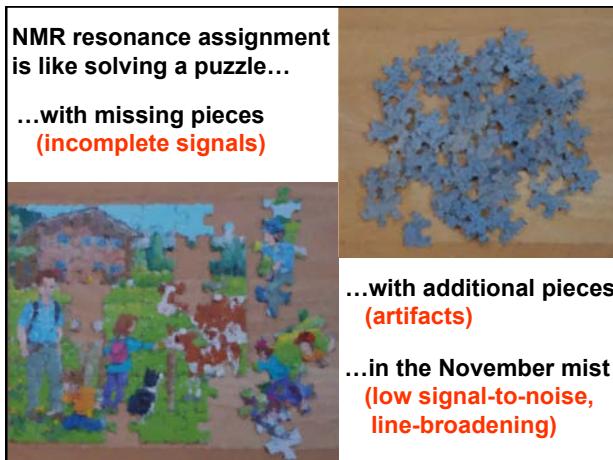
How to set the calibration constant?

- Known distances (intraresidual or in standard secondary structures)
- Preliminary structure, if available
- User-defined value for the average (median) upper distance limit

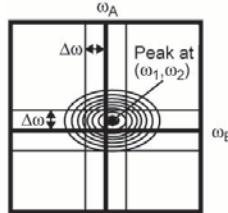


Problems when interpreting NOEs

- Internal motion
- Spin diffusion
- Spectral overlap
- Chemical shift degeneracy
- Time consuming spectral analysis, if done manually → automation



Ambiguity of chemical shift based NOE assignment

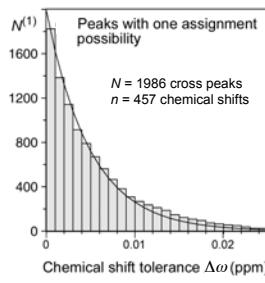


In general, several different ^1H chemical shifts ω_A , ω_B match the position of a NOESY peak within the experimental uncertainty $\Delta\omega$.

→ Assignment ambiguity

Manual assignment is very cumbersome!

NOEs with a unique chemical shift based assignment



2D NOESY:

$$N^{(1)} \approx N \exp(-4n \Delta\omega / \Delta\Omega)$$

3D NOESY:

$$N^{(1)} \approx N \exp(-2n \Delta\omega / \Delta\Omega)$$

$N^{(1)}$ Number of uniquely assigned peaks

N Number of cross peaks

n Number of chemical shifts

$\Delta\omega$ Chemical shift tolerance

$\Delta\Omega$ Spectrum width

Ambiguous distance restraints

$$d_{\text{eff}} = \left(\sum_k d_k^{-6} \right)^{-1/6} \leq b$$

upper distance bound

distance for assignment possibility k

sum over all assignment possibilities

- Restraint with multiple assignments
- If one assignment possibility leads to a sufficiently short distance, then the ambiguous distance restraint will be fulfilled.
- The presence of wrong assignment possibilities has no (or little) influence on the structure, as long as the correct assignment possibility is present.

Nilges et al., *J. Mol. Biol.* 269, 408–422 (1997)

Properties of ambiguous distance restraints

$$d_{\text{eff}} = \left(\sum_k d_k^{-6} \right)^{-1/6}$$

- d_{eff} is never longer than any of the individual distances d_k :
 $d_{\text{eff}} \leq d_k$ for all k
- d_{eff} is close to the smallest individual distance:
 $d_{\text{eff}} \approx d_1$ if $d_1 \ll d_2, d_3, \dots$
- Examples: $d_1 = 3 \text{ \AA}$, $d_2 = 10 \text{ \AA}$ → $d_{\text{eff}} = 2.9996 \text{ \AA}$
 $d_1 = 3 \text{ \AA}$, $d_2 = \dots = d_{10} = 10 \text{ \AA}$ → $d_{\text{eff}} = 2.9967 \text{ \AA}$

3J skalare Kopplungen

NMR Daten: Aufspaltung eines Signals
Konformationsdaten: Einschränkungen von Torsionswinkeln, θ

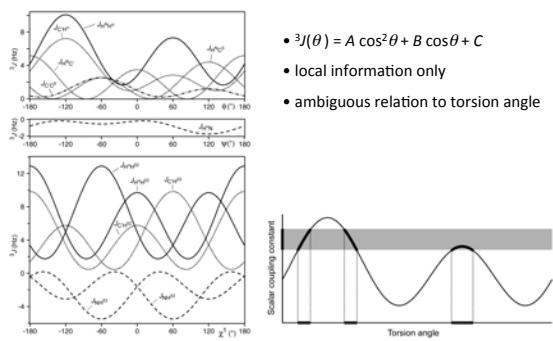
Karplus-Kurve: $^3J(\theta) = A \cos^2 \theta + B \cos \theta + C$
mit empirischen Konstanten A, B, C

Zum Beispiel: $^3J_{\text{HNH}\alpha}(\phi)$, $^3J_{\text{H}\alpha\text{H}\beta}(\chi^2)$

Eigenschaften:

- Information nur über lokale Konformation
- mehrdeutige Beziehung $^3J \leftrightarrow \theta$

3J scalar couplings



H-Brücken

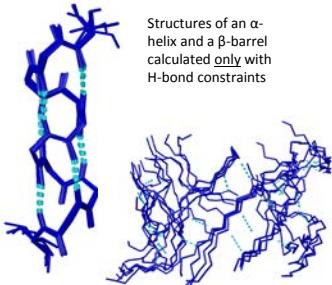
NMR Daten: langsamer $^1\text{H} \rightarrow ^2\text{H}$ Austausch + NOEs
Konformationsdaten: Donor-Akzeptor Distanz

Typische H-Brücken: -N-H ↔ O=C- in regulären Sekundärstrukturen (Helices, β -Blätter)

Eigenschaften:

- Bzgl. Sequenz mittel- und langreichweitig
- Donor (H) identifizierbar
- Akzeptor (O) i. A. nur indirekt bestimmbar (benachbarte NOEs + Annahmen über Sekundärstruktur)

Impact of hydrogen bond restraints



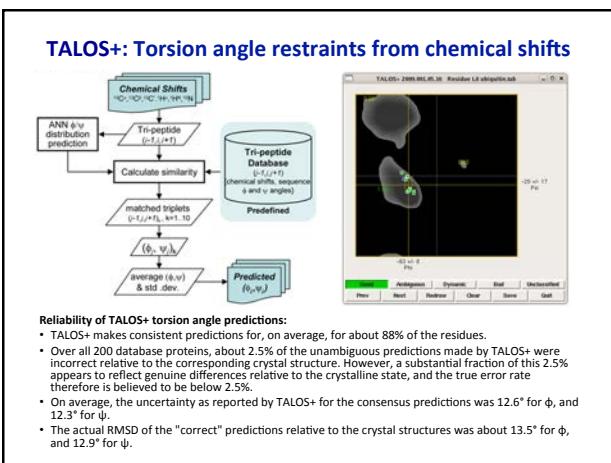
- Strong impact on structure
- Direct detection of H-bonds by NMR is possible, but not sensitive
- Without identification of acceptor atom ≈ assumption on secondary structure

Chemische Verschiebungen

NMR Daten: chem. Verschiebungen, δ
Konformationsdaten: (ϕ, ψ) Torsionswinkelbereiche
Komplexe Beziehung: $\delta \leftrightarrow (\phi, \psi)$

Eigenschaften:

- einfache Messung
- (ϕ, ψ) -Werte aus Datenbank von Proteinen mit bekannter Struktur und chem. Verschiebungen (TALOS)
- Information über lokale Konformation bzw. Sekundärstruktur



Residuelle dipolare Kopplungen (RDC)

NMR Daten: Zusätzliche Signalaufspaltung bei partieller Molekülausrichtung, z.B. $^1J_{\text{NH}} \rightarrow ^1J_{\text{NH}} + D_{\text{NH}}$

Konformationsdaten: Orientierung von Bindungen relativ zur Molekülausrichtung

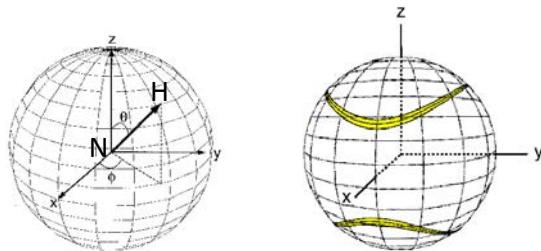
Residuelle dipolare Kopplung: $D(\theta, \phi) = A [(3\cos^2\theta - 1) + 3/2 R \sin^2\theta \cos 2\phi]$

A, R Amplitude (Betrag) und Rhombizität (Abweichung von Rotationssymmetrie) des Ausrichtungstensors
 θ, ϕ Richtung der Bindung relativ zum Ausrichtungstensor (Polarkoordinaten)

Eigenschaften:

- Proteinprobe in schwach ausrichtendem Medium (Flüssigkristalle/Bizellen, fadenförmige Phagen, komprimierte Gele)
- Information über globale Konformation,
- z.B. relative Ausrichtung von Domänen
- Entartung: 1 Messwert \rightarrow Doppelkegel von Richtungen
- Bestimmung des Ausrichtungstensors (A, R)?

Residuelle dipolare Kopplungen



$$D(\theta, \phi) = A [(3\cos^2\theta - 1) + 3/2 R \sin^2\theta \cos 2\phi]$$

Strukturberechnungs-algorithmen

Ist NMR Strukturberechnung möglich?

- Grundsätzlich:
 - NOEs messen nur kurze Distanzen < 5 Å
 - ungenaue obere Schranken
 - Kann damit die globale Struktur eines 30 Å langen Proteins bestimmt werden?
JA, wenn genügend Daten vorhanden sind.
- Praktisch:
 - Zielfunktion hat viele lokale Minima
 - Kann eine (fast) optimale Struktur gefunden werden?
JA.

Strukturberechnungsalgorithmen

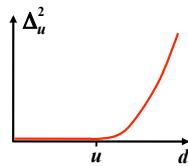
- Frühere Methoden:
 - Interaktiver Modellbau
 - Distanzgeometrie
 - Minimierung einer variablen Zielfunktion
- Simulated annealing:
 - Monte Carlo
 - Moleküldynamiksimulation im kartesischen Raum
 - Moleküldynamiksimulation im Torsionswinkelraum

CYANA target function

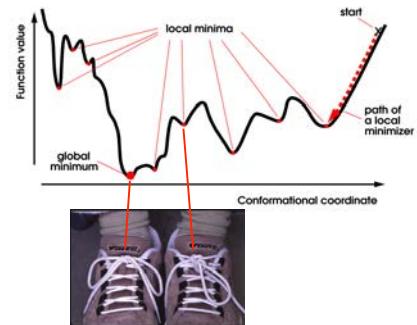
$$T = \sum_{\text{upper distance limits (NOEs)}} \Delta_u^2 + \sum_{\text{lower distance limits (steric)}} \Delta_l^2 + \sum_{\text{torsion angle restraints}} \Delta_a^2 + \dots$$

$\Delta_u, \Delta_l, \Delta_a$: restraint violations,

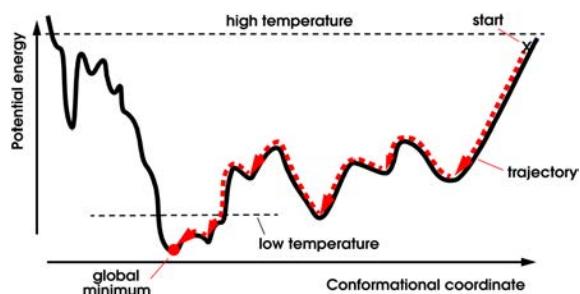
e. g., $\Delta_u = \begin{cases} d - u & \text{if } d > u \\ 0 & \text{otherwise} \end{cases}$



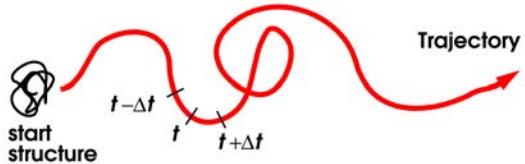
Target function = potential energy



Simulated annealing



Molecular Dynamics Simulation



Numerical integration of classical equations of motion

Integration of the equations of motion

e.g. "leap-frog" algorithm

$$q(t + \Delta t) = q(t) + \Delta t \dot{q}(t + \Delta t/2) + O(\Delta t^3)$$

$$\dot{q}(t + \Delta t/2) = \dot{q}(t - \Delta t/2) + \Delta t \ddot{q}(t) + O(\Delta t^3)$$

q coordinates (Cartesian or torsional)

$\dot{q} = \frac{dq}{dt}$ velocities

$\ddot{q} = \frac{d^2q}{dt^2}$ accelerations

Δt time step

Atomkoordinaten Torsionswinkel

Strukturbeschreibung

Atomkoordinaten (kartesische Koordinaten):

- 3 Freiheitsgrade pro Atom
- abhängig von der Wahl des Koordinatensystems
- beinhalten auch "unwichtige" Freiheitsgrade
- einfach

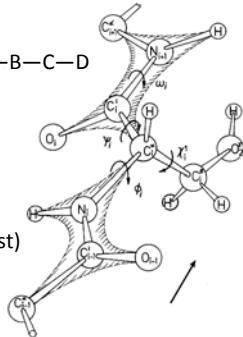
Torsionswinkel (= Diederwinkel, Dihedralwinkel):

- Drehungen um Einfachbindungen
- interne Koordinaten
- essentielle Freiheitsgrade
- Bindungslängen, Bindungswinkel fest
- kompliziertere aber effizientere Algorithmen

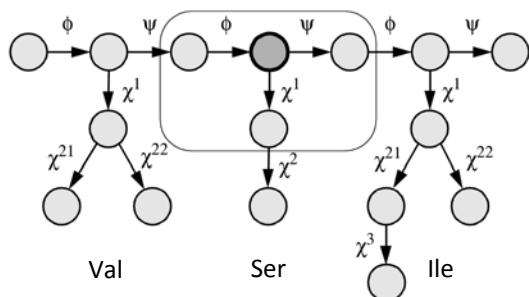
Torsionswinkel

- Definiert durch 4 Atome: A—B—C—D
- Drehung um Bindung B—C
- Werte von -180° bis +180°

- Torsionswinkel von AS i:
- $\phi_i: C'_{i-1}—N_i—C^\alpha_i—C'_i$
- $\psi_i: N_i—C^\alpha_i—C'_i—N_{i+1}$
- $\omega_i: C^\alpha_i—C'_i—N_{i+1}—C^\alpha_{i+1}$ (fest)
- $\chi'_i: N_i—C^\alpha_i—C^\beta_i—C^\gamma_i$



Torsionswinkel: Baumstruktur



MD Simulation im Torsionswinkelraum "Torsionswinkeldynamik"

- Klassische Mechanik
- N Torsionswinkel als einzige Freiheitsgrade
- Etwa 10 Mal weniger Freiheitsgrade als im kartesischen Raum.
- Feste Bindungslängen und -winkel:
→ "Einfrieren" der schnellsten Bewegungen
→ Längere Zeitschritte

Jain, Vaidehi, Rodriguez, *J. Comp. Phys.* 106, 258–268 (1993)
Güntert, Mumenthaler, Wüthrich, *J. Mol. Biol.* 273, 283–298 (1997)

Equations of motion

Cartesian coordinates: x_1, \dots, x_N

$$m_i \ddot{x}_i = - \frac{\partial E_{\text{pot}}}{\partial x_i} \quad (\text{Newton})$$

Generalized coordinates: q_1, \dots, q_n

$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_k} \right) - \frac{\partial L}{\partial q_k} = 0 \quad (\text{Lagrange})$$

with $L = E_{\text{kin}} - E_{\text{pot}}$

Molecular Dynamics

Cartesian space

$$E_{\text{kin}} = \frac{1}{2} \sum_{i=1}^N m_i \dot{x}_i^2 \quad \begin{array}{l} \text{Kinetic} \\ \text{energy} \end{array}$$

diagonal, constant
(elements m_i)

$\ddot{x}_i = \frac{1}{m_i} \frac{\partial E_{\text{pot}}}{\partial x_i}$

proportional to N

Torsion angle space

$$E_{\text{kin}} = \frac{1}{2} \sum_{k,l=1}^n M(\theta_{kl}) \dot{\theta}_k \dot{\theta}_l$$

Mass matrix
 M

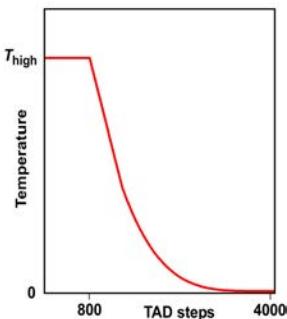
$M(\theta) \ddot{\theta} = C(\theta, \dot{\theta})$
(n linear equations)

solving linear system
of equations: $\sim n^3$

exploiting tree structure
of the molecule: $\sim n$

Simulated annealing protocol

- Start from random structure
- Use all restraints simultaneously
- Adjustable parameters:
 - start temperature, T_{high}
 - number of TAD steps



Temperature control

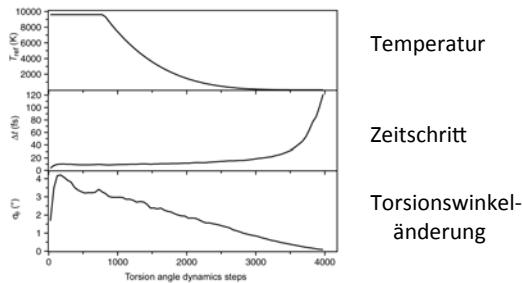
Weak coupling to a heat bath is used to control the temperature:

$$\dot{\theta} \leftarrow \dot{\theta} \sqrt{1 + \frac{T^{\text{ref}} - T}{\tau T}}$$

$\dot{\theta}$ torsional velocities
 T instantaneous temperature, $T = \frac{2E_{\text{kin}}}{nk_B}$
coupling constant

(Berendsen et al., J. Chem. Phys. 81, 3684–3690, 1984)

Simulated annealing mit Torsionswinkeldynamik

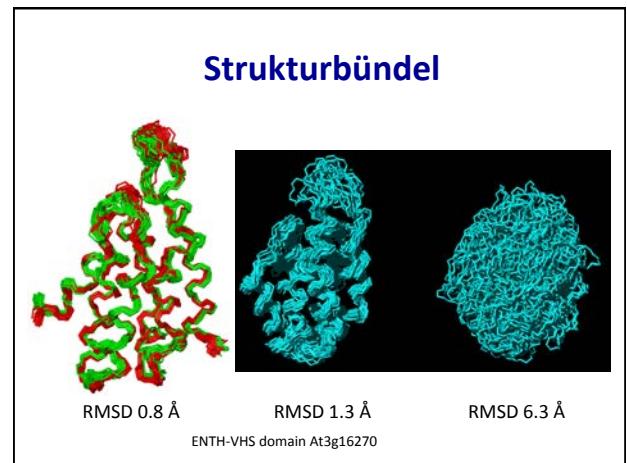


Strukturbündel RMSDs

Strukturbündel

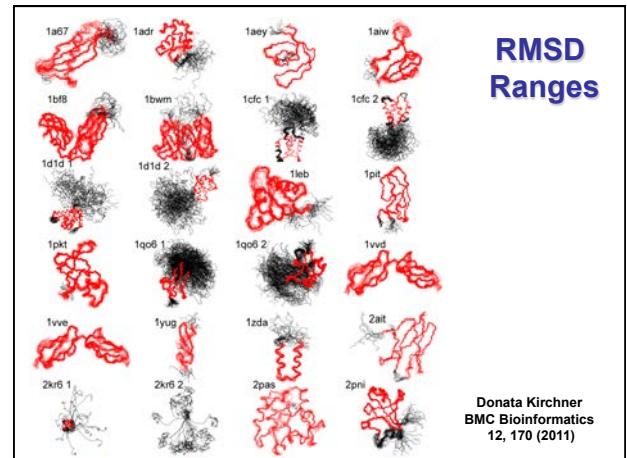
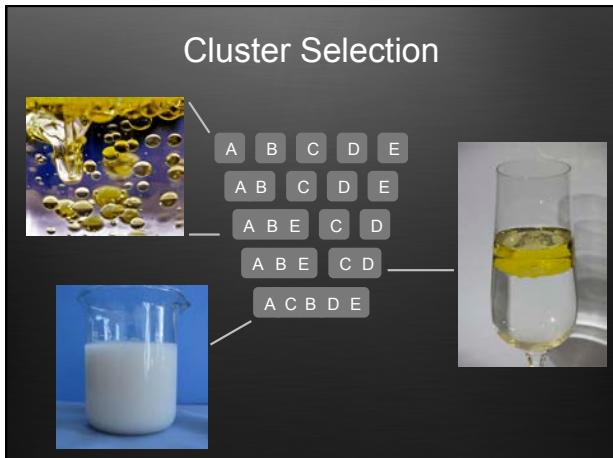
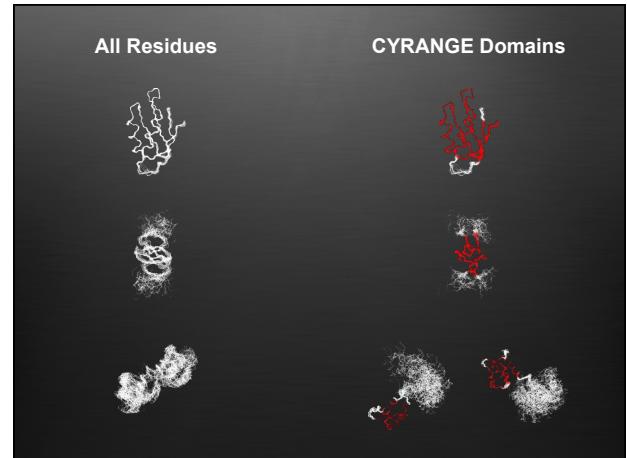
- 100 Startstrukturen mit zufälligen Torsionswinkel
- 100 unabhängige simulated annealing Läufe mit:
 - gleichen experimentellen Daten
 - unterschiedlichen Startstrukturen
- Auswahl der 20 “besten” Strukturen mit den tiefsten Zielfunktionswerten
- Sampling des Konformationsraums?

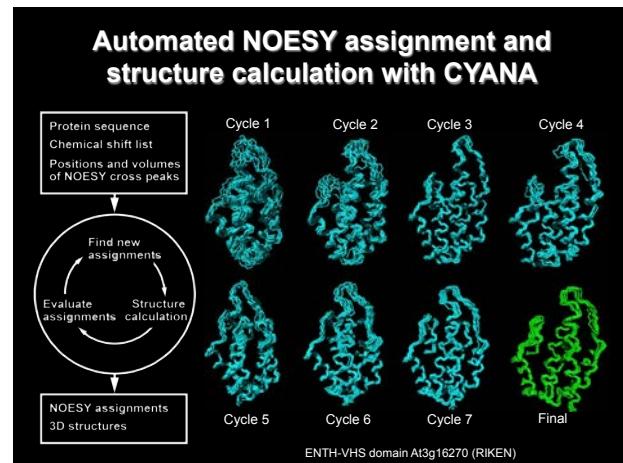
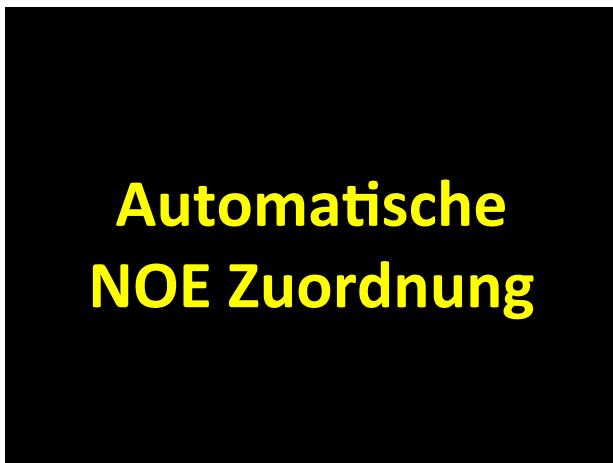




RMSD (root-mean-square deviation)

- Zwei Strukturen mit n Atomen und Koordinaten $\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n$ und $\mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_n$
- $$RMSD = \min_{R, \vec{t}} \sqrt{\frac{1}{n} \sum_{i=1}^n |\vec{x}_i - R\vec{y}_i - \vec{t}|^2}$$
- Minimum über alle Rotationen R und Translationen $\vec{t} \rightarrow$ optimale Überlagerung



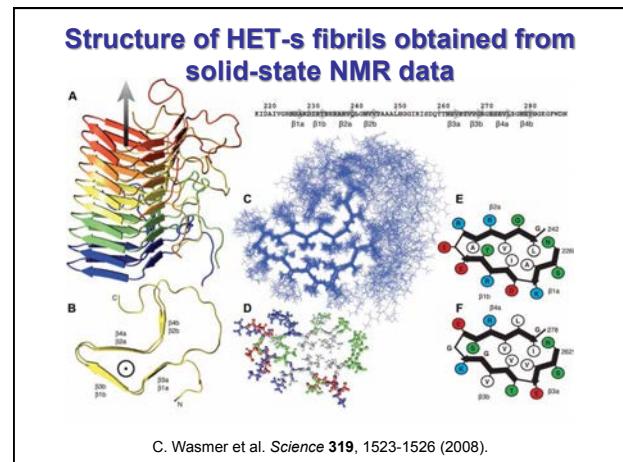
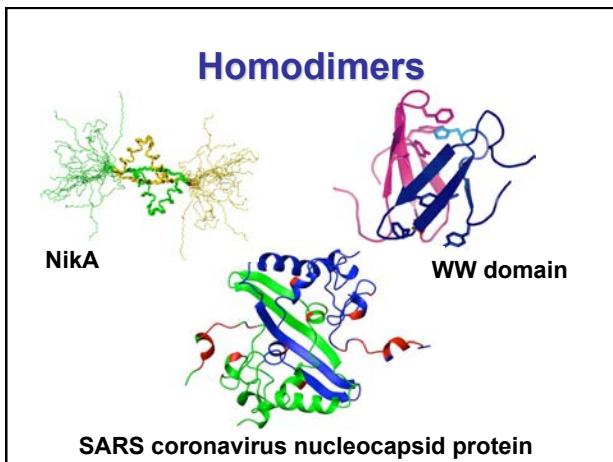


Output overview table							
Cycle	1	2	3	4	5	6	7 Final
Peaks:							
selected	: 5439	5439	5439	5439	5439	5439	5439
with assignment	: 5100	4806	4742	4749	4712	4678	4675
without assignment	: 339	633	697	690	727	761	764
with diagonal assignment	: 12	12	12	12	12	12	12
Cross peaks:							
with unique diagonal assignment	: 5088	4794	4730	4737	4700	4666	4663
with unique assignment	: 675	3591	3872	4115	4195	4194	
with short-range assignment i-j <=1:	: 3295	3208	3165	3154	3120	3022	3089
with medium-range assignment 1< i-j <5 :	: 1020	925	921	914	904	884	893
with long-range assignment i-j >5:	: 773	661	644	669	676	680	681
Upset distance limits:							
total:	: 3786	2986	2832	2789	2707	2643	2683
short-range, i-j <1	: 2007	1596	1486	1440	1386	1340	1273
medium-range, 1< i-j <5	: 1220	959	787	775	726	760	765
long-range, i-j >5:	: 559	451	559	574	568	569	650
Average assignments/restraint	: 4.81	1.73	1.27	1.25	1.18	1.14	1.00
Average target function value	: 230.84	69.79	68.20	9.22	3.99	2.98	1.70
RMSD (residues 15..130):							
Average backbone RMSD to mean	: 1.34	0.97	0.57	0.67	0.68	0.60	0.53
Average heavy atom RMSD to mean	: 1.76	1.44	1.09	1.19	1.20	1.07	0.98
0.53							1.01

CYANA Computation Time

- Combined NOE assignment and structure calculation of a 114 amino acid residue protein with the program CYANA:
- 8 cycles × 100 conformers = **800 structures**
- 10000 torsion angle dynamics steps per conformer
- Linux cluster system with Quad-core Intel Xeon E5462 (2.8 GHz, 12 MB cache), 2 GB memory/core

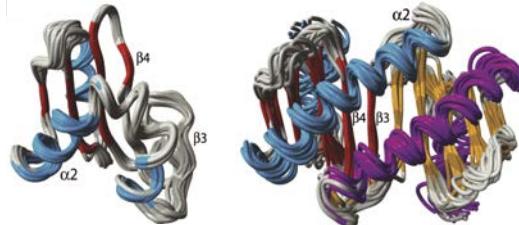
Processors	Computation time (s)
100	147
50	217
25	354
10	769



Strukturanalyse Validierung

Correct and wrong structure: Dynein light chain 2A

Wrong structure (1TGQ) Correct structure (1Y4O): Homodimer



Nabuurs, S. B., Spronk, C. A. E. M., Vuister, G. W. & Vriend, G. (2006). Traditional biomolecular structure determination by NMR spectroscopy allows for major errors. *PLoS Comp. Biol.*, 2, 71–79.

Validation principles

Agreement of the three-dimensional structure with

- Experimental data
- Unused experimental data: cross-validation
- Physical principles
- Empirical knowledge about protein structures

Validation of the

- Local structure
- Global structure

Absolute/relative validation:

- Is my structure correct? ("absolute")
- Is structure A more likely to be correct than structure B? ("relative")

X-ray crystallography: R-factor

- Measures agreement between measured data (reflections) and 3D structure
- Definition: Relative difference between structure factors, $F(hkl)$, that were observed (F_{obs}) and back-calculated from the 3D structure (F_{calc}):

$$R = \frac{\sum |F_{obs}| - |F_{calc}|}{\sum |F_{obs}|} \quad \text{with } I_{hkl} \propto |F(hkl)|^2$$

I_{hkl} = intensity of reflection (hkl)

- Perfect agreement: $R = 0$
Good protein X-ray structure: $R < 0.2$
Random structure: $R \approx 0.6$

X-ray: Free R-factor

- Use, say, 90% of the data (reflections) for the structure determination
- Use the remaining 10% to compute the R value → "free" R value, obtained from independent data
- Detects errors better than conventional R -factor
- Each reflection influences whole electron density
- Many reflections → No problem to omit 10% of the reflections from the structure determination

Brünger, A. T. (1992). Free R value: a novel statistical quantity for assessing the accuracy of crystal structures. *Nature* 355, 472-475.

R-factor in NMR

- NMR restraints (NOEs) are not raw data but require assignments, calibration, etc.
- Back-calculation of NOEs from 3D structures needs data or assumptions on dynamics and consideration of spin diffusion → "Relaxation matrix calculations"
- Agreement between measured and back-calculated NOESY peak volumes:
 - dominated by strong short-range NOEs
 - absence/presence of a weak (but structurally important!) long-range NOE has negligible influence on the R -factor
- Agreement of distances?

Free R-factor using RDCs

- Use NOE distance restraints to determine structure
- Use residual dipolar couplings to validate
- Quality factor (*R*-factor):

$$Q = \text{rms}(D^{\text{calc}} - D^{\text{obs}})/\text{rms}(D^{\text{obs}}),$$

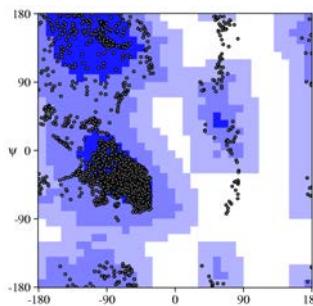
where D^{obs} and D^{calc} are observed and calculated one-bond dipolar couplings.

Simon, K., Xu, J., Kim, C. & Skrynnikov, N. (2005). Estimating the accuracy of protein structures using residual dipolar couplings. *J. Biomol. NMR* 33, 83-93.

Validation without experimental data

- Stereochemical quality
- “Normality” of the structure with respect to the existing structures in Protein Data Bank
- Parameters:
 - Bond lengths, bond angles
 - Ramachandran plot
 - Steric overlap (“bumps”)
- Conformational energy
- **3D structure (molecular graphics!)**

Ramachandran-Plot



Example:
Each black dot = 1 residue in 1 conformer
 • 73% in most favored regions (dark blue)
 • 21% in additionally allowed regions (light blue)
 • 4% in generously allowed regions (blue-grey)
 • 2% in disallowed regions (white)

(Programm PROCHECK)

WHAT_CHECK validation checks

- **Administrative checks:** nomenclature, missing atoms
- **Geometry:** chirality, bond lengths, bond angles, torsion angles (evaluation, Ramachandran plot, omega, χ^1/χ^2), rings and planarity, proline puckering
- **Structure:** inside/outside profile, bumps, packing, backbone (number of hits, backbone normality, peptide flips), sidechain rotamers
- **Hydrogen bonds:** unsatisfied, flip check, His assignments
- **Summary:** overall Z-scores and RMS Z-scores

$$Z = \frac{X_i - \langle X \rangle}{\sigma(X)} \quad \text{RMS-Z} = \sqrt{\langle Z^2 \rangle}$$

WHAT_IF/WHAT_CHECK output

- Structure Z-scores, positive is better than average:
 1st generation packing quality : 0.891
 2nd generation packing quality : 1.444
 Ramachandran plot appearance : -0.105
 chi-1/chi-2 rotamer normality : -0.431
 Backbone conformation : 0.551
- RMS Z-scores, should be close to 1.0:
 Bond lengths : 0.887
 Bond angles : 1.143
 Omega angle restraints : 0.437 (tight)
 Side chain planarity : 0.934
 Improper dihedral distribution : 1.053
 B-factor distribution : 3.497 (loose)
 Inside/Outside distribution : 0.930

Hooft, R. W. W., Vriend, G., Sander, C., Abola, E. E. (1996) Errors in protein structures. *Nature* 381, 272.

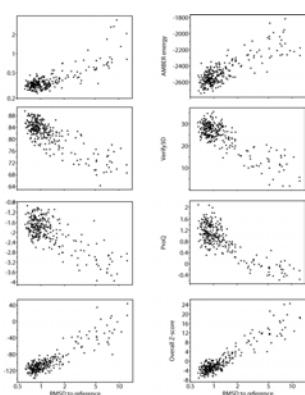
Correlation between validation parameters and structure accuracy

- 252 ubiquitin structure bundles calculated with CYANA (FLY)A
- Accuracy = RMSD from reference structure
- 7 quality parameters, S_i
- Overall Z-score:

$$Z = \sum_{i=1}^7 \frac{S_i - \bar{S}_i}{\sigma(S_i)}$$

Correlation coefficient 93%

Teppei Ikeya

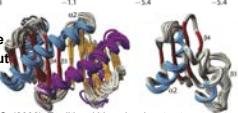


Quality indicators for correct and wrong structures of DLC2A

Table 1. Average Quality Indicators of the 1Y4O and 1TGQ Structure Ensembles before and after Refinement in Explicit Solvent

Criteria	Characteristic	1Y4O (Original)	1Y4O (Refined)	1TGQ (Original)	1TGQ (Refined)
Agreement with experimental data	RMS violation: non-existent restraints (\AA)	0.0129	0.0097	0.007	0.0284
	Violations > 0.5 Å 1Y4O distance restraints	0	0	0.5	0
	RMS violation 1TGQ _{obs} restraints (\AA)	12.8	12.6	0.321	0.0231
	Violations > 0.5 Å 1TGQ _{obs} restraints	32	32	4	0
PROCHECK validation results ^a	RMS violation: non-existent dihedral restraints (\AA)	0.497	0.336	23.0	1.59
	Violations > 5° 1Y4O dihedral restraints	0	0	34	4
	Most favored regions	91.2	90.5	67.7	85.8
	Additionally allowed regions	8.4	9.0	27.3	12.8
WHAT IF structure Z-scores ^b	Generalized allowed regions	0.2	0.2	4.7	0.5
	Disallowed regions	0.2	0.3	0.2	0.9
	Packing quality	-0.4	0.1	-2.1	-1.5
	Ramachandran plot appearance	-3.9	-3.1	-6.6	-4.6
WHAT IF structure Z-scores ^b	χ_1/χ_2 Helix-turn-helix	-0.3	-0.7	5.6	-3.0
	Backbone conformation	-0.8	-1.1	-5.4	-2.4

• Better quality indicators for correct structure
 • But difficult to detect wrong structure without knowledge of correct structure



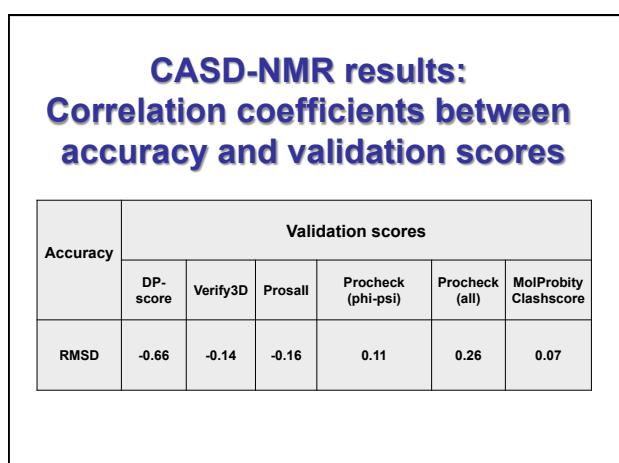
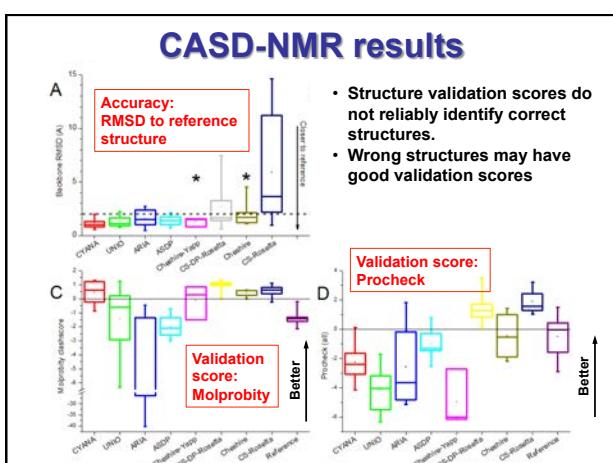
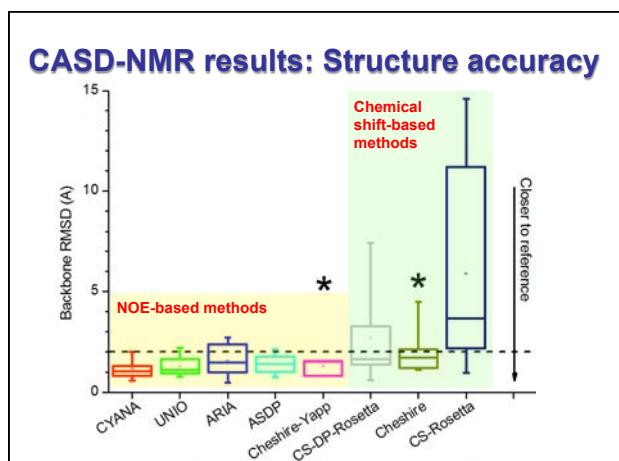
Nabuurs, S. B., Spronk, C. A. E. M., Vuister, G. W. & Vriend, G. (2006). Traditional biomolecular structure determination by NMR spectroscopy allows for major errors. *PLoS Comp. Biol.*, 2, 71–79.



CASD-NMR: Critical Assessment of Structure Determination by NMR

- Evaluation of current algorithms for automated NOESY assignment and structure calculation
- Blind test (analogous to CASP):
 - NMR data are provided 8 weeks before the release of the structure by the PDB.
 - Structures obtained by different algorithms are collected before the original PDB structure is released.
- Open to anybody for providing data and for calculating structures by automated methods
 - In 1st round: 10 protein NMR data sets, 7 algorithms.

<http://wenmr.eu/wenmr/casd-nmr>
 Rosato, A. et al., *Nature Methods* 6, 625–626 (2009)



Unterlagen zur Vorlesung

<http://www.bpc.uni-frankfurt.de/guentert/wiki/index.php/Teaching>